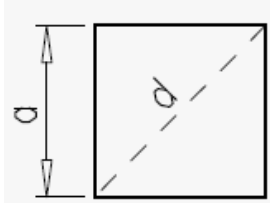


## Grundlagen Geometrie - Flächen

A = Fläche    d = Diagonale / Durchmesser    h = Höhe    U = Umfang    r = Radius

Quadrat



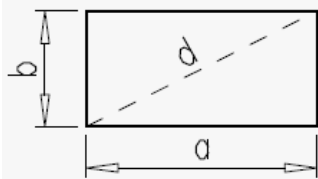
$$A = a^2$$

$$a = \sqrt{A}$$

$$d = a\sqrt{2}$$

$$U = 4 \cdot a$$

Rechteck

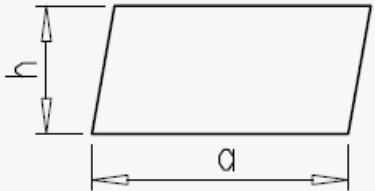


$$A = a \cdot b$$

$$d = \sqrt{a^2 + b^2}$$

$$U = 2 \cdot a + 2 \cdot b$$

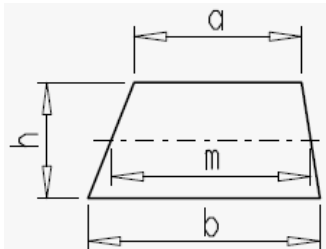
Parallelogramm



$$A = a \cdot h$$

$$a = \frac{A}{h}$$

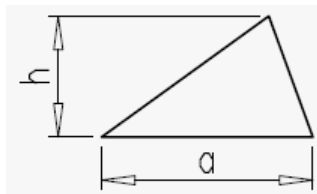
Trapez



$$A = m \cdot h$$

$$m = \frac{a + b}{2}$$

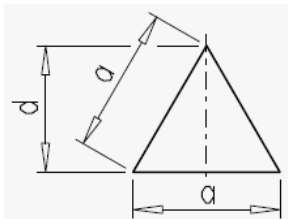
Dreieck



$$A = \frac{1}{2} \cdot a \cdot h$$

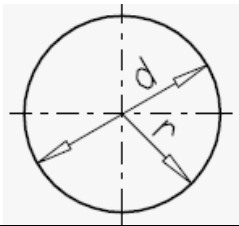
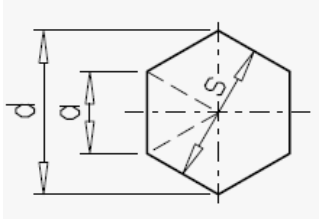
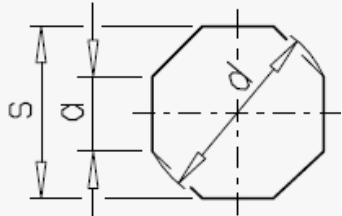
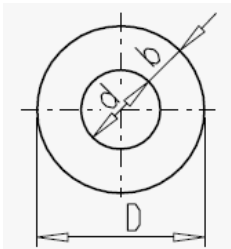
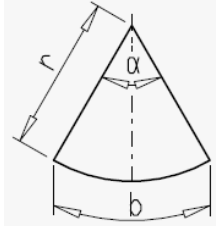
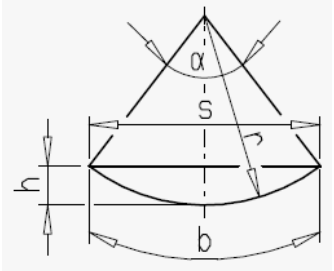
$$a = \frac{2 \cdot A}{h}$$

Gleichseitiges Dreieck



$$A = \frac{a^2}{4} \sqrt{3}$$

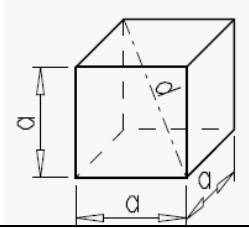
$$d = \frac{a}{2} \sqrt{3}$$

<p>Kreis</p> 	$A = \frac{d^2 \cdot \pi}{4} = \pi \cdot r^2 \approx 0,785 \cdot d^2$ $U = 2 \cdot r \cdot \pi = \pi \cdot d$ $d = 2 \cdot r$
<p>Sechseck</p> 	$A = \frac{3 \cdot a^2 \cdot \sqrt{3}}{2}$ $d = 2 \cdot a$ $s = \sqrt{3} \cdot a$
<p>Achteck</p> 	$A = 2 \cdot a^2 (\sqrt{2} + 1)$ $d = a \cdot \sqrt{4 + 2\sqrt{2}}$ $s = a(\sqrt{2} + 1)$
<p>Kreisring</p> 	$A = \frac{\pi}{4} \cdot (D^2 - d^2) = (d + b)b \cdot \pi$ $b = \frac{D - d}{2}$
<p>Kreisausschnitt</p> 	$A = \frac{r^2 \cdot \pi \cdot \alpha^\circ}{360^\circ} = \frac{b \cdot r}{2}$ $b = \frac{r \cdot \pi \cdot \alpha^\circ}{180^\circ}$
<p>Kreisabschnitt</p> 	$A = \frac{r^2}{2} \left( \frac{\alpha^\circ \cdot \pi}{180^\circ} - \sin \alpha \right) = \frac{1}{2} [r(b - s) + sh]$ $s = 2r \cdot \sin \frac{\alpha}{2}$ $h = r \left( 1 - \cos \frac{\alpha}{2} \right) = \frac{s}{2} \tan \frac{\alpha}{4}$ $\hat{\alpha} = \frac{\alpha^\circ \cdot \pi}{180^\circ}$ $b = r \cdot \hat{\alpha}$

## Grundlagen Geometrie - Volumina

V = Volumen   O = Oberfläche   M = Mantel   h = Höhe   A = Fläche   r = Radius   d/D = Durchmesser

Würfel

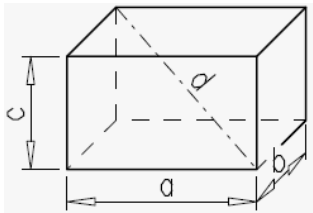


$$V = a^3$$

$$O = 6 \cdot a^2$$

$$d = a\sqrt{3}$$

Quader

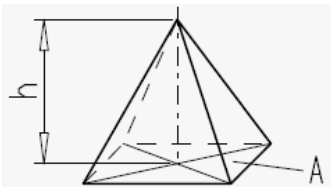


$$V = a \cdot b \cdot c$$

$$O = 2(ab + ac + bc)$$

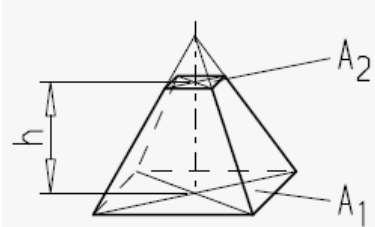
$$d = \sqrt{a^2 + b^2 + c^2}$$

Pyramide



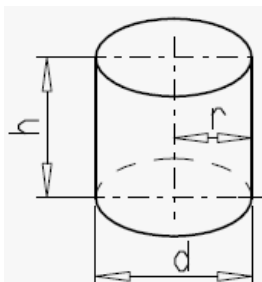
$$V = \frac{A \cdot h}{3}$$

Pyramidenstumpf



$$V = \frac{h}{3} (A_1 + A_2 + \sqrt{A_1 \cdot A_2})$$

Zylinder

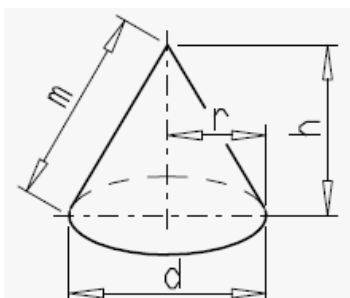


$$V = \frac{h \cdot \pi}{4} (D^2 - d^2)$$

$$M = 2 \cdot \pi \cdot r \cdot h$$

$$O = 2 \cdot r \cdot \pi \cdot (r + h)$$

Kegel

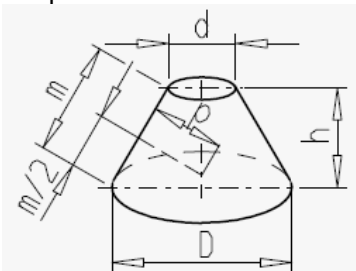
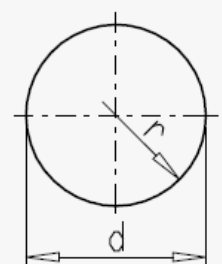
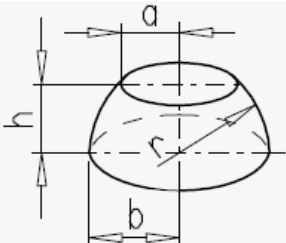
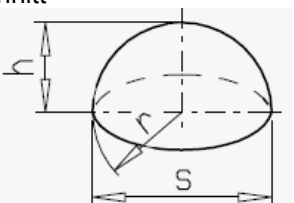
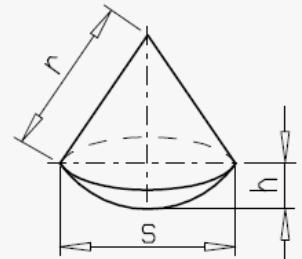
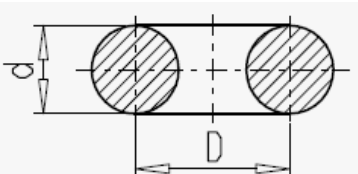


$$V = \frac{r^2 \cdot \pi \cdot h}{3}$$

$$M = r \cdot \pi \cdot m$$

$$O = r \cdot \pi \cdot (r + m)$$

$$m = \sqrt{h^2 + \left(\frac{d}{2}\right)^2}$$

<p>Kegelstumpf</p> 	$V = \frac{\pi \cdot h}{12} (D^2 + Dd + d^2)$ $M = \frac{\pi \cdot m}{2} (D + d) = 2 \cdot \pi \cdot p \cdot h$ $m = \sqrt{\left(\frac{D-d}{2}\right)^2 + h^2}$
<p>Kugel</p> 	$V = \frac{4}{3} r^3 \pi = \frac{1}{6} \cdot d^3 \pi \approx 4,189 \cdot r^3$ $O = 4\pi \cdot r^2 = \pi \cdot d^2$
<p>Kugelzone</p> 	$V = \frac{\pi \cdot h}{6} (3a^2 + 3b^2 + h^2)$ $M = 2 \cdot \pi \cdot r \cdot h$
<p>Kugelabschnitt</p> 	$V = \frac{\pi \cdot h}{6} \left(\frac{3}{4}s^2 + h^2\right) = \pi h^2 \left(r - \frac{h}{3}\right)$ $M = 2 \cdot r \cdot \pi \cdot h = \frac{\pi}{4} (s^2 + 4h^2)$
<p>Kugelausschnitt</p> 	$V = \frac{2}{3} \cdot h \cdot r^2 \cdot \pi$ $O = \frac{\pi \cdot r}{2} (4h + s)$
<p>Kreisring</p> 	$V = \frac{D \cdot \pi^2 \cdot d^2}{4}$ $O = D \cdot d \cdot \pi^2$